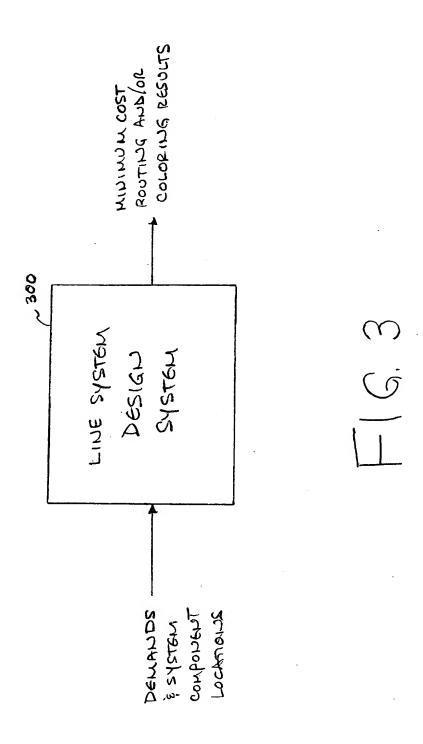


مي اهم

Special Case	problem Complexity	(L, *, E), s = 2 polynomial		(L, *, NE), s = 2 polynomial	(L, U, E), $s = 2$ 4/3-Approx	(L, D, *), s = 3 NP-hard		(S)	
	Approx upper bound	$O(\sqrt{s})$ $(L,$	2	2 (L,*			$2(1+\epsilon)$		16.2
General Case	Approx lower bound	$\Omega(\sqrt{s})$	$1 + 1/s^2$	NP-hard	in-approximable	in-approximable	NP-hard	€	
	problem	(L, D, *)	(L,U,NE)	(L,U,E)	(C, *, NE)	(C,D,E)	(C,U,E)		



```
Methodology A
m(o) = 0
for p = 1 to line system load/<sub>2</sub>
        1(p) = 0; m(p) = m(p-1) + 2;
        for i = 1 to n - 1
                 l_i(p) \leftarrow load on link e_i
                 if(l_i(p) = 0)
                         Divide the line system into two line systems;
                         one from node 0 to node (i - 1); the other from
                         node i to node (n - 1) and call methodology A
                         on these line systems separately.
                 if(l_i(p) > l(p))
                         l(p) = l_i(p)
        create a multigraph G = (V, E), where V = \{0, ...n - 1\}
        for all demand (i, j) in D
                 create an edge (i - 1, j) in G
        for i = 1 to n - 1
                 if l_{i}(p) < l(p)
                         add an edge (i - 1, i) in G
        set the capacity of each edge in G to 1
        find a 2-unit flow from node 0 to node (n - 1) in G
        Let p1 and p2 be the path for the flow
        For all the demands corresponding to links in p1.
        {
                 Assign the color c_{m(p)} to demand
                 remove the demand from D
        For all the demands corresponding to links in p2
                 Assign the color c_{m(p)+1} to demand
                 remove the demand from D
        }
```

F16.4A

. }

```
Routing Phase:
     if (L(R_s) \ge n(1+\epsilon)/\epsilon)
          Output R<sub>s</sub>
     else {
          Compute D_1 = \{d \in D | d \text{ in any routing goes through at least } n/3 \text{ links } \}
          Compute D_2 = D - D_1
          Compute R_1 = the set of all possible routings for demands in D_1
          Compute R_2 = the set of all possible routings for demands in D_2
          in which at most 3S demands are not routed on shortest paths
          Compute R = R_1 \times R_2
          Compute r \in R such that L(r) = \min_{r' \in R} L(r')
          Output r
     }
Coloring Phase:
            U = D
            M = the set of availabale colors
            l = \min_{e_i \in L} l_i(U) (the min. load of demands in U)
             while (l > 0) {
                 Compute O = H(U) (see Edica)
                  Compute m = \{i, j | i, j \text{ are the smallest two colors in } M \}
                 Color demands in O with colors in m
                 U = U - O
                 M = M - m
                 l = \min_{e_i \in L} l_i(U)
            if (U \neq \emptyset) {
                 Color U using methodologyA
    "Compute 0 = H(U)":
  Compute d_0 = a demand in U that goes through the largest number of links in L
  O = \{d_0\}
  L' =  set of links covered by demands in O
  i = 1
  while (L' \neq L) {
       Compute D_i = \{d | d \in U - O \& d \text{ overlaps with } d_{i-1}\}
       Compute d_i = \{d | d \in D_i \& d \text{ goes through the largest number of links in } L - L'\}
       i = i+1
  output O
```

F16.4B

Methodology B:

```
e_0 = (-1, 0)
e_{n+1}=(n,n+1)
L=L\cup\{e_0,e_{n+1}\}
D = D \cup \{(0,0), (n+1,n+1)\}
for all (0 \le i \le j \le n+1) {
     P(i,j)=\emptyset
     R(i,j) = \emptyset
     best = 0
     for all (i \le i' \le j' \le j) {
           E_1 = \{e_i, e_{i+1}, \dots e_{i'}\} \cup \{e_{j'+1}, e_{j'+2}, \dots e_j\}
           E_2 = \{e_{i'+1}, e_{i'+2}, \dots e_{j'}\}
           Compute coloring C using rection by 1 where E_1 (E_2) links are colored with 1 (2)
           steps
           if(C \neq \emptyset) {
                if(i'-i+j-j'+1 \ge best) \ \{
                      R(i,j)=C
                      best = i' - i + j - j' + 1
                 }
            }
      }
       Compute L_1 = \{e_i | e_i \in L, l_i \leq |C_1|\}
       for all (e_i, e_j \in L_1) {
            Compute D_{i,j} = \{d | d \in D, d \text{ goes through either link } e_i, e_j\}
            Compute P_{i,j} = coloring obtained by coloring the interval graph D_{i,j} with colors in C_1
       for all (e_i, e_j \in L_1, i < j) {
            best = 0
            for all(m, i < m < j) {
                  Compute the coloring K = P(i, m) + P(m, j)
                  If (K = \emptyset) continue
                  Compute n = \text{number of links that are in one step in } K
                  if (best < n) {
                       best = n
                        C = K
                  }
             Compute n = number of links that are in one step in R(i, j)
             if (best < n) {
                  best = n
                  C = R(i, j)
             P(i,j)=C
        Output P(0, n+1)
```

F16.4C

Methodology 61:

Compute C = interval graph coloring of demands D_1 using colors in C_1 if $(C == \emptyset)$ Output C Compute C' = interval graph coloring of the demands in $D - D_1$ using first available colors Output $C' \cup C$

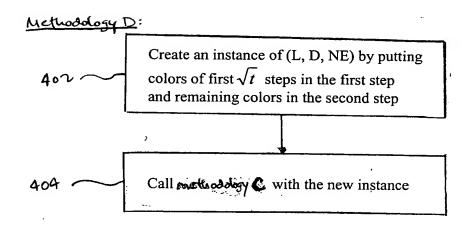
FIG. 4D

Methodology c1:

```
V = \{0, 1, \dots, n-1\}

E = \emptyset
for all demands ((i, j) \in D - D_1) {
     E = E \cup \{(i-1,j)\}
     Directed link (i-1,j) has unit capacity
for all links (e_i \in L) {
     E = E \cup \{(i-1,i)\}
     Directed link (i-1,i) has capacity |C_1| + |C_2| - l_i
Graph G = (V, E)
Compute maxFlow = Max. Flow f in G from node 0 to node n-1
if(maxFlow < |C_2|) Output \emptyset
Compute F_1 = \{d \mid f \text{ puts zero flow on the edge } (i-1,j) \text{ where demand } d = (i,j)\}
Compute F_1 = F_1 \cup D_1
Compute K_1 = coloring that colors demands in F_1 with colors in C_1 only using interval graph
coloring
Compute K_2 = coloring that colors demands in D - F_1 with colors in C_2 only using interval
 graph coloring
 Output K = K_1 \cup K_2
```

FIG 4E



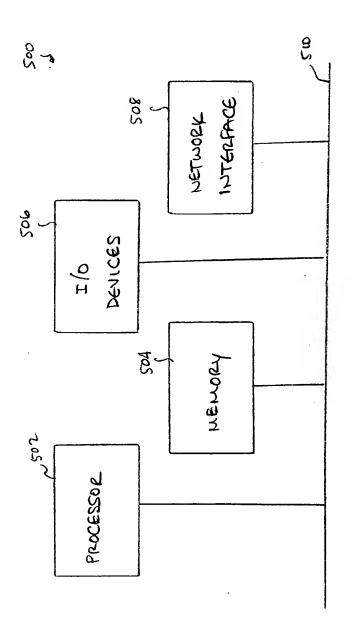
F16.4F

Create solution O₁ by doing an interval graph coloring of D with colors C₁ U C₂

Create a solution O₂ by calling reflected by B

Output the cheapest cost solution among O₁ & O₂

F16.46



T.G. 5